

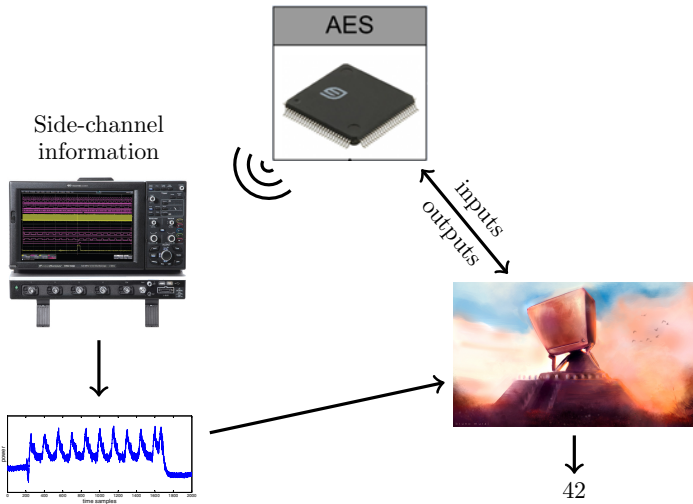
# Strong 8-bit Sboxes with Efficient Masking in Hardware

18<sup>th</sup> August, 2016.

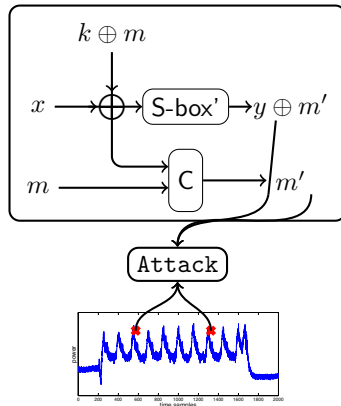
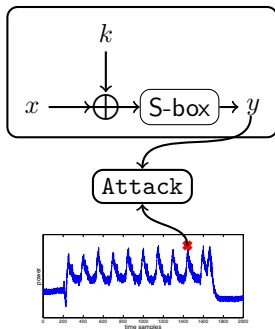
Erik Boss<sup>1</sup> Vincent Grosso<sup>1</sup> Tim Güneysu<sup>2</sup>  
Gregor Leander<sup>1</sup> Amir Moradi<sup>1</sup> Tobias Schneider<sup>1</sup>

<sup>1</sup>Horst Görtz Institute for IT Security, Ruhr-Universität Bochum, Germany

<sup>2</sup>University of Bremen and DFKI, Germany

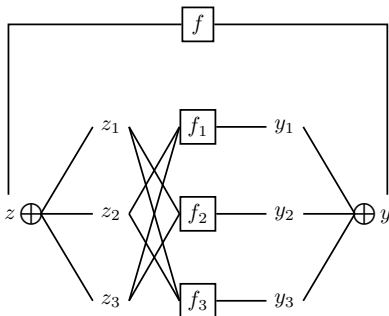


# Masking: principle



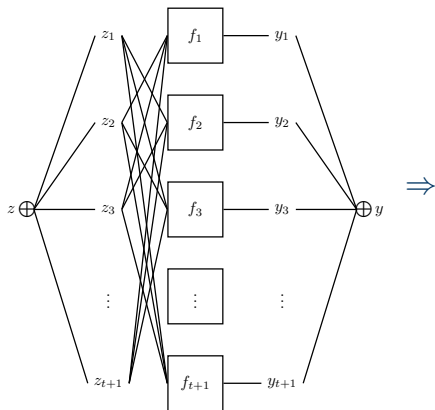
- Expecting: number of measurements grows up exponentially in the number of shares with noise as a basis
- Security conditions
  - Noise
  - Randomness
  - Independence of the leakages: possible issue in hardware due to glitches

# Threshold implementations



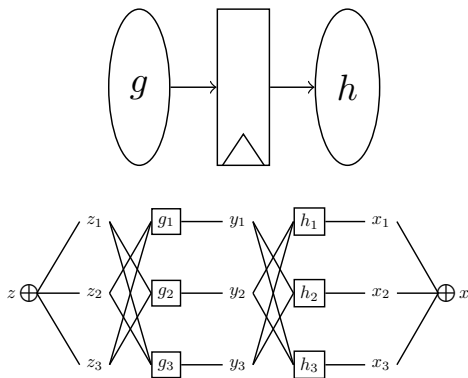
- **Correctness:** the shared functions compute the actual function
- **Non-completeness:** each sub-circuit is independent of one share
- **Uniformity:** the output of the shared function is a uniform sharing (use fresh randomness if needed)

Number of shares for TI:  
degree of  $f + 1$

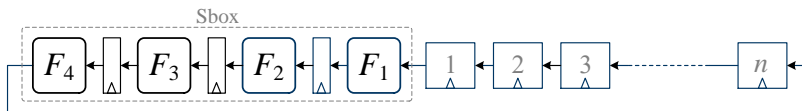


$\Rightarrow$

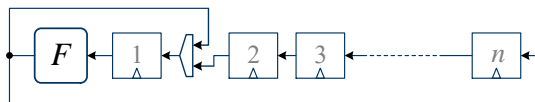
$$f = h \circ g$$



## Different implementation techniques



Raw



Iterative

# Previous work

- Exhaustive search for small S-boxes (i.e.  $n \leq 4$ )  
4-bit S-boxes: 302 bijective classes  $\Rightarrow$  35 efficient TI with 3 shares [CHES 2012]
- Look for interesting S-boxes and try to find a nice threshold implementation, e.g.:
  - AES [EUROCRYPT 2011, Africacrypt 2014] 8-bit
  - Fides [CHES 2013] 5-bit, 6-bit
  - Keccak [CARDIS 2013] 5-bit
- Large S-box with good cryptographic/threshold implementation properties?



Use results for small S-boxes to find TI of larger S-boxes

Use results for small S-boxes to find TI of larger S-boxes

Lot of existing S-boxes use small S-boxes to build larger one

- CLEFIA
- Crypton
- Fantomas
- ICEBERG
- Khazad
- Robin (iterative implementation)
- Scream v3
- Whirlpool

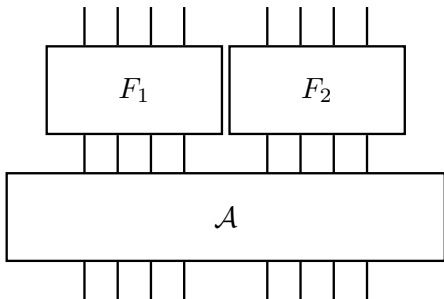
Use results for small S-boxes to find TI of larger S-boxes

Lot of existing S-boxes use small S-boxes to build larger one

- CLEFIA
- Crypton
- Fantomas
- ICEBERG
- Khazad
- Robin (iterative implementation)
- Scream v3
- Whirlpool

Can we achieve better results? Can we take advantage of iterative implementation?

## From small to large S-box: SPN

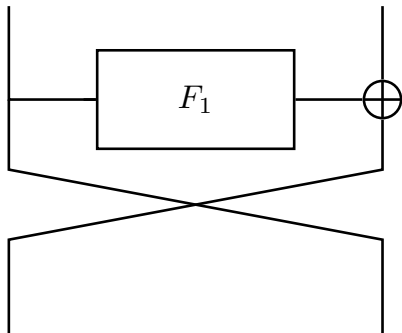


Structure used for: Iceberg, Khazad, Whirlpool,...

- 16! choices for  $F_1$  and  $F_2$   
 →  $F_1, F_2$  easy to share  
 4-bit S-box → 35
  - $\mathcal{A}$  bit permutation 8!
  - $\mathcal{A}$   $\mathbb{F}_{16}$ -linear layer 61200
- Constant: 256

$$\text{Cost} \simeq 2^{32}$$

## From small to large S-box: Feistel



Structure used for: Robin,  
Scream v3,...

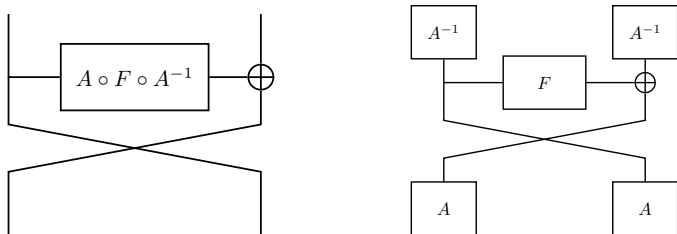
Structure well studied up to 3  
rounds

- $2^{64}$  choices for  $F_1$

Feistel gives uniformity for “free” (if  $F_1$  can be computed in one clock cycle)

## Reduce the search space

Affine equivalence:  $F_1 = A \circ F \circ B + C$



Reduce the search space from all function  $2^{64}$  to function of the  $A \circ F + C$

- $F$  is an instance of an affine class
- $A$  is an affine permutation
- $C$  is a linear mapping

Cost  $\simeq 2^{46.5} \Rightarrow$  use GPUs

- Bijective
- Non-linearity
- Differential uniformity
- Algebraic degree

	Diff.	Lin.	Deg.	Threshold Implementation			Type	
				Area[GE] Iter.	Stage #	Mask #		
AES	Best Known			4244	5	48	Inversion	
				3708	3	44		
	4	32	7	3653	3	44		
				2835	3	32		
Whirlpool	8	56	7	2203	9	0	SPN	
SB <sub>4</sub> (this work)	8	56	7	202	1507	5	0	Feistel
SB <sub>3</sub> (this work)	8	60	7	273	1498	4	0	SPN
ICEBERG	8	64	7	2115	9	0	SPN	
Khazad	8	64	7	2062	9	0	SPN	
Scream v3	8	64	6	2204	6	0	Feistel	
Fantomas	16	64	5	766	4	0	SPN	
Robin	16	64	6	319	1180	6	0	Feistel
SB <sub>1</sub> (this work)	16	64	6	51	1189	8	0	SPN
SB <sub>2</sub> (this work)	16	64	4	253	631	2	0	SPN



	Diff.	Lin.	Deg.	Threshold Implementation			Type	
				Area[GE] Iter.	Stage #	Mask #		
AES	Best Known			4244	5	48	Inversion	
				3708	3	44		
	4	32	7	3653	3	44		
				2835	3	32		
Whirlpool	8	56	7	2203	9	0	SPN	
SB <sub>4</sub> (this work)	8	56	7	202	1507	5	0	Feistel
SB <sub>3</sub> (this work)	8	60	7	273	1498	4	0	SPN
ICEBERG	8	64	7	2115	9	0	SPN	
Khazad	8	64	7	2062	9	0	SPN	
Scream v3	8	64	6	2204	6	0	Feistel	
Fantomas	16	64	5	766	4	0	SPN	
Robin	16	64	6	319	1180	6	0	Feistel
SB <sub>1</sub> (this work)	16	64	6	51	1189	8	0	SPN
SB <sub>2</sub> (this work)	16	64	4	253	631	2	0	SPN

Same round functions allow us to make iterative implementation

	Diff.	Lin.	Deg.	Threshold Implementation			Type	
				Area[GE] Iter.	Stage #	Mask #		
AES	Best Known			4244	5	48	Inversion	
				3708	3	44		
	4	32	7	3653	3	44		
				2835	3	32		
Whirlpool	8	56	7	2203	9	0	SPN	
SB <sub>4</sub> (this work)	8	56	7	202	1507	5	0	Feistel
SB <sub>3</sub> (this work)	8	60	7	273	1498	4	0	SPN
ICEBERG	8	64	7	2115	9	0	SPN	
Khazad	8	64	7	2062	9	0	SPN	
Scream v3	8	64	6	2204	6	0	Feistel	
Fantomas	16	64	5	766	4	0	SPN	
Robin	16	64	6	319	1180	6	0	Feistel
SB <sub>1</sub> (this work)	16	64	6	51	1189	8	0	SPN
SB <sub>2</sub> (this work)	16	64	4	253	631	2	0	SPN

Interesting tradeoff for different implementation

	Diff.	Lin.	Deg.	Threshold Implementation			Type	
				Area[GE] Iter.	Stage #	Mask #		
AES	Best Known			4244	5	48	Inversion	
				3708	3	44		
	4	32	7	3653	3	44		
				2835	3	32		
Whirlpool	8	56	7	2203	9	0	SPN	
SB <sub>4</sub> (this work)	8	56	7	202	1507	5	0	Feistel
SB <sub>3</sub> (this work)	8	60	7	273	1498	4	0	SPN
ICEBERG	8	64	7	2115	9	0	SPN	
Khazad	8	64	7	2062	9	0	SPN	
Scream v3	8	64	6	2204	6	0	Feistel	
Fantomas	16	64	5	766	4	0	SPN	
Robin	16	64	6	319	1180	6	0	Feistel
SB <sub>1</sub> (this work)	16	64	6	51	1189	8	0	SPN
SB <sub>2</sub> (this work)	16	64	4	253	631	2	0	SPN

No 8-bit balanced Feistel with identical round functions up to 5 iterations achieve better cryptographic properties than SB<sub>4</sub>

- Various S-boxes with decent cryptographic properties and efficient TI
- Even for unprotected implementation they are efficient (cf. the paper)
- Some S-boxes have also good behavior for (masked) bitslice implementation (cf. the paper,  $SB_2$  have similar number of AND gates as Robin and Scream v3)

Thanks!

Questions?